A Quick Review of a few Topics from Calculus 3- HW Problems

1. Find a vector equation and parametric equations for a line passing through (-1, 2, 3) in the direction of  $\vec{v} = \vec{\iota} + 2\vec{j} - \vec{k}$ .

2. Find a vector equation of a line through the points (2, -3, 1) and (-1, 1, 4).

3. Calculate  $\|\vec{v}\|$ ,  $\|\vec{w}\|$ , and  $\vec{v} \cdot \vec{w}$ , if  $\vec{v} = <1, 2, -2 >$  and  $\vec{w} = <-2, 3, 1 >$ .

4. Find a unit vector in the direction of  $\vec{v} = < -1, -2, 2 >$ .

5. Find all values of x such that the vectors  $\vec{v} = <1, x, x >$  and  $\vec{w} = <5, -6, x >$  are perpendicular.

6. Find an equation of a plane that passes through the points (2, 1, 1), (3, 3, 2), (5, -2, -2).

7. Sketch a rough graph of the following equations in  $\mathbb{R}^3$ .

a. 
$$z = 4x^{2}$$
  
b.  $z = 4x^{2} + 4y^{2}$   
c.  $z^{2} = 4x^{2} + 4y^{2}$ 

*d*. 
$$1 = 4x^2 + 4y^2$$

 $e. \quad 4x^2 + 4y^2 + 4z^2 = 64.$