Some Substitution Methods and Exact Equations- HW Problems

In problems 1-3 show the equation is exact and find the general solution to the differential equation.

1.
$$(2x^2 - 3y^2)dx + (y^2 - 6xy)dy = 0$$

2.
$$(\cos(x) + \ln(y))dx + \left(\frac{x}{y} + e^y\right)dy = 0$$

3.
$$\left(x^3 + \frac{y}{x}\right) + \left(y^2 + \ln(x)\right)\frac{dy}{dx} = 0.$$

In problems 4-6 find the general solution to the differential equation.

$$4. \quad xy' = y + 2\sqrt{xy}$$

5.
$$(xy)y' - x^2 - y^2 = 0$$

$$6. \quad x^2y' = xy + y^2$$

In problems 7 and 8 find the general solution by reducing the order of the differential equation.

7.
$$y'' = 2(y')^2$$

8.
$$x^2y'' + 4xy' = 1$$