First Order Linear Differential Equations- HW Problems

In problems 1 and 2 find the general solution to the differential equations.

1.
$$(x^2 + 1)\frac{dy}{dx} + 2xy - 3x = 0$$

2.
$$xy' + y = 4\sqrt{x}$$
; $x > 0$.

In problems 3-7 solve the initial value problems.

3.
$$\frac{dy}{dx} = -2xy + 2xe^{(-x^2)}; \quad y(0) = 2$$

4.
$$xy' = 2y + x^3 \sin(x)$$
; $y(1) = 0$

5.
$$(x^2 + 1)y' + 5xy = x;$$
 $y(0) = 2$

6.
$$xy' + 4y = \frac{e^{-x}}{x^3}$$
; $y(1) = 0$, $x > 0$

7.
$$(1+x)y' + y = \cos(x)$$
; $y(0) = 1$, $1+x > 0$.