The Change of Variables Theorem- HW Problems

Evaluate the following integrals.

1.
$$\iint_D (x^2 + y^2)^2 dA; \text{ where } D \text{ is the disk } x^2 + y^2 \le 9.$$

- 2. $\iint_D (x^2 + y^2)^2 dA;$ where *D* is the annulus $1 \le x^2 + y^2 \le 4$.
- 3. $\iint_D (x^2 + y^2)^2 dA;$ where *D* is the part of the annulus $1 \le x^2 + y^2 \le 4$ where $x \ge 0$.
- 4. $\iiint_W (e^{(x^2+y^2)}+2z)dV$ where W is part of the solid cylinder $x^2 + y^2 \le 9$ where $1 \le z \le 2$. Hint: cylindrical coordinates.
- 5. $\iiint_W (\sqrt{x^2 + y^2 + z^2}) dV$ where W is the set where $x^2 + y^2 + z^2 \le 4$. Hint: spherical coordinates.

6.
$$\iiint_{W} (\sqrt{x^{2} + y^{2} + z^{2}}) dV \quad \text{where } W \text{ is the solid bounded by} \\ x^{2} + y^{2} + z^{2} = 1, \quad x^{2} + y^{2} + z^{2} = 4, \\ \text{and } z = 0, \text{ with } z \ge 0.$$

 $7. \quad \int_0^\infty e^{-9x^2} dx.$

8. Find the volume of the solid that lies inside the sphere $x^2 + y^2 + z^2 = 4$ and outside the cylinder $x^2 + y^2 = 1$. Hint: cylindrical coordinates.

9. Evaluate $\iiint_W \left(e^{\left(x^2 + y^2 + z^2\right)^{\frac{3}{2}}} \right) dV$ where W is bounded by $x^2 + y^2 + z^2 = 1$ and $z = \frac{1}{2}$ with $\frac{1}{2} \le z \le 1$.