

Directional Derivatives and Gradients- HW Problems

Find the directional derivative at the given point in the direction of \vec{v} .

1. $f(x, y) = e^{xy} + x^2 + y^2$ at $(1, 2)$, $\vec{v} = -4\vec{i} + 3\vec{j}$
2. $f(x, y) = xy^2 + x^3y$ at $(-1, 1)$, $\vec{v} = \vec{i} + \vec{j}$
3. $f(x, y, z) = x^3y^2 + e^{(y+z)} - 2x\sin(z)$ at $(1, 0, 0)$, $\vec{v} = 2\vec{i} - 2\vec{j} + \vec{k}$

4. Find a vector perpendicular to the curve $x^2 - 2xy + y^3 = 5$ at $(1, 2)$.

Find the tangent plane and normal line to the surface at the given point.

5. $x^2 + y^2 - z^2 + 2xy - 2xz = 2$ at $(-1, 2, 1)$.
6. $xe^y + y^2 + z^2 = 7$ at $(-2, 0, 3)$

7. The electrical potential V at a point in space is given by $V(x, y, z) = 4x^2 + 2xz - xyz$.

- a. Find the rate of change of V at the point $A(1, 2, -3)$ in the direction $\vec{v} = \vec{i} - \vec{j} + \vec{k}$.
- b. In which direction does V change the fastest at $A(1, 2, -3)$?
- c. What is the maximum rate of change of V at $A(1, 2, -3)$?