Infinite Limits and Limits at Infinity- HW Problems

1. Using the limit definition prove the following limits:

a.
$$\lim_{x \to 1} \frac{1}{(x-1)^2} = +\infty$$

b.
$$\lim_{x \to -3} \frac{-1}{(x^2 - 9)^2} = -\infty$$

$$c. \quad \lim_{x \to \infty} (x^3 - x^2) = +\infty$$

d.
$$\lim_{x \to -\infty} \frac{x}{2x+1} = \frac{1}{2}$$

e.
$$\lim_{x\to\infty}e^{-x}=0.$$