## Compact Sets and Connected Sets- HW Problems

1. Which of the sets A though I in HW problem #6 in the section called Metric Spaces- Definitions and Examples are compact?

2. Let  $E, F \subseteq X, d$  be compact subsets of a metric space X. Just using the definition of compactness (i.e., you can't use the theorem that says a union of compact sets in compact) prove the  $E \cup F$  is a compact subset of X.

3. Let  $E_1, E_2, ..., E_n \subseteq X, d$  be compact subsets of a metric space X. Just using the definition of compactness prove that  $E_1 \cup E_2 \cup ... \cup E_n$ , where n is a positive integer, is a compact subset of X.

4. Let  $p_1$  and  $p_2$  be points in a metric space X. Prove that the set  $p_1 \cup p_2$  is compact in X.

5. Let  $p_1, p_2, p_3, ..., p_n$  be points in a metric space X. Prove that the set  $p_1 \cup p_2 \cup p_3 \cup ... \cup p_n$ , where n is a positive integer, is compact in X.

6. Prove that the open set (0,2) is not a compact subset of  $\mathbb{R}$  by finding an open cover with no finite subcover.